

Modeling Fixed-Income Securities and Interest Rate Options

SECOND EDITION

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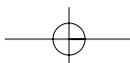
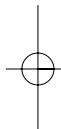
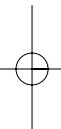
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